

# **THE KNUDSEN COMPRESSOR AS AN ENERGY EFFICIENT MICRO-SCALE VACUUM PUMP**

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# Overview

- Knudsen Compressor Description
- Advantages of Thermal Transpiration Pumps
- Thermal Transpiration Pump History at USC
- Transitional Flow Formulation and Results
- Sample Stage Sizing and Performance
- Special Considerations at the Low Pressure Limit
- Summary

# Thermal Effusion and Creep

Rarefied gas phenomena (free-molecular flow driven by gas-surface interactions)

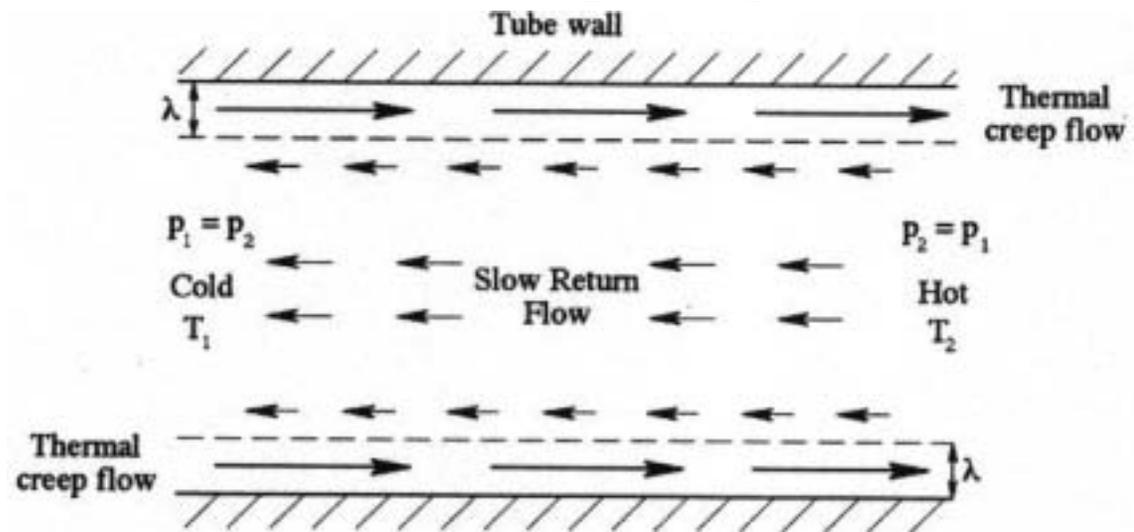
## Thermal Effusion Through Orifice

$$T_1 < T_2$$

$P_1, T_1$	$P_2, T_2$
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$$\frac{p_1}{p_2} = \sqrt{\frac{T_1}{T_2}}$$

## Thermal Creep along surfaces



- Longitudinal Wall temperature gradient drives creep flow, counterbalanced by pressure driven return flow (Poiseuille flow)

- One of the driving mechanisms in Crooke's radiometer

Net effect is a flow from cold to hot side of tube

# Knudsen Compressor Stage Operation

$$TMPD = \frac{\nabla P / P}{\nabla T / T}$$

Flow in a Knudsen Compressor is the difference between thermal creep and pressure driven return flows

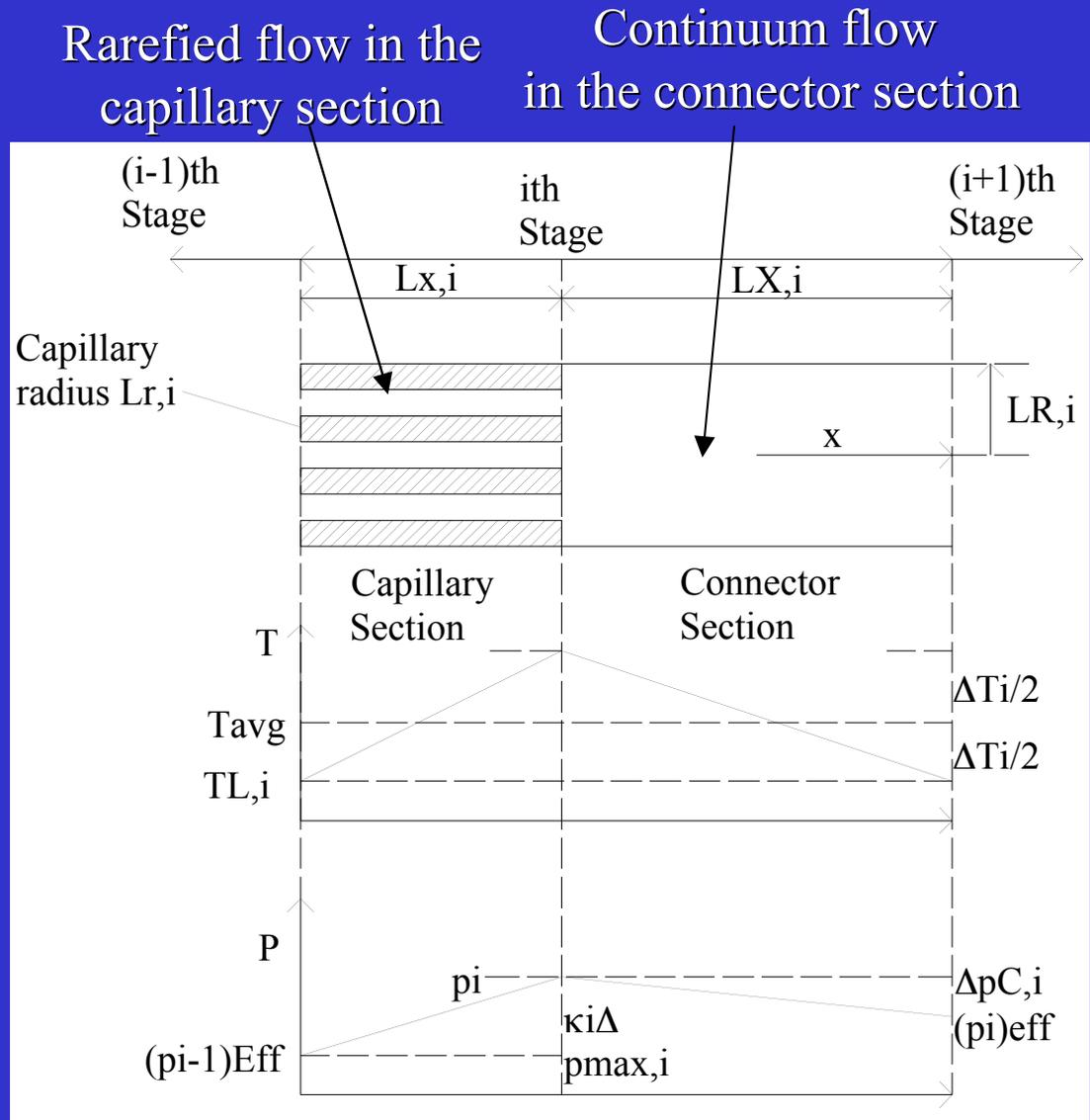
## FM equations

$$N_T = \left\{ \frac{\sqrt{\pi}}{12} n_v v_o d^3 \right\} \frac{\nabla T}{T}$$

$$N_p = \left\{ -\frac{\sqrt{\pi}}{6} n_v v_o d^3 \right\} \frac{\nabla p}{p}$$

$$TMPD_{FM} = -$$

$$TMPD_{Cont} = 0$$

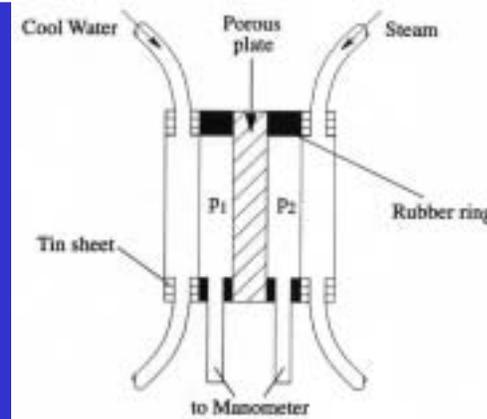


# Why Thermal Transpiration Pumps?

- No moving parts.
- No oil or working fluids.
- Recent availability of small pore membrane materials with very low thermal conductivities.
- Can operate on waste heat from other equipment.
- MEMS fabrication allows for batch fabrication of the many required stages.
- Can operate over a wide range of pressures.
  - Roughing pump from 10 mTorr – 1 atm
  - High pressure gas source from 1 atm to 10 atm

# Time-Line for Thermal Transpiration Pumps

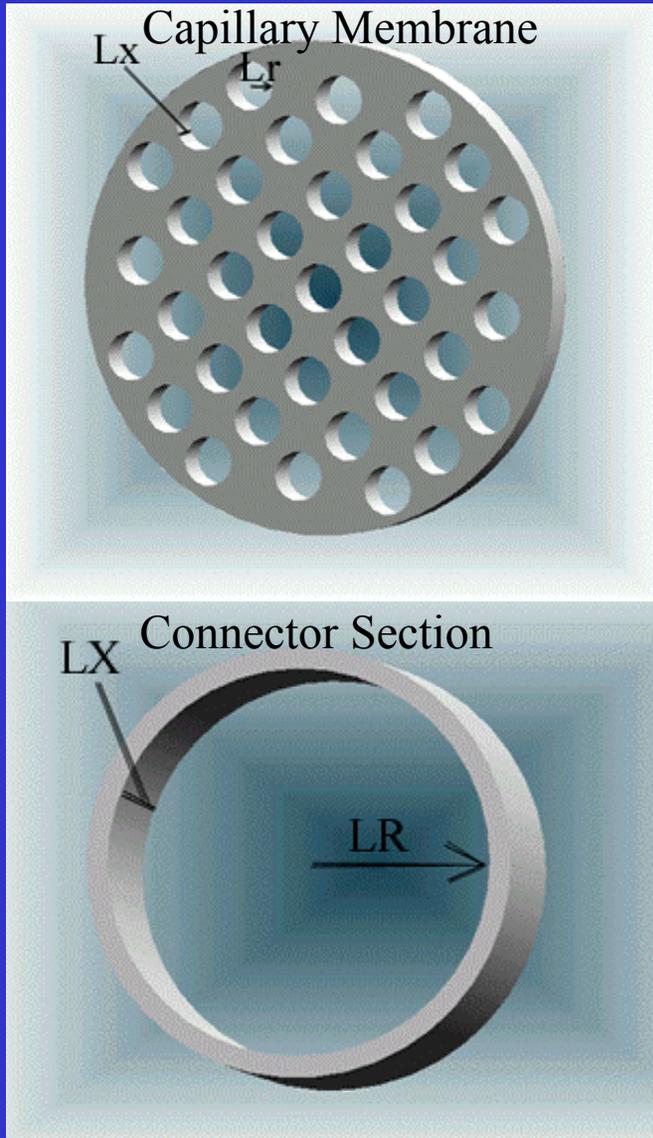
- Reynolds -- first explained thermal transpiration



- Knudsen -- experimentally achieved pressure ratio of 10 with first multiple stage pump based on thermal transpiration.
- Pham-Van-Diep – Analysis of MEMS based pump
- Vargo – Demonstrated MEMS based vacuum pump stages
- MEMS Knudsen Pump – Optimize and Construct Multistage MEMS vacuum pump suitable for application



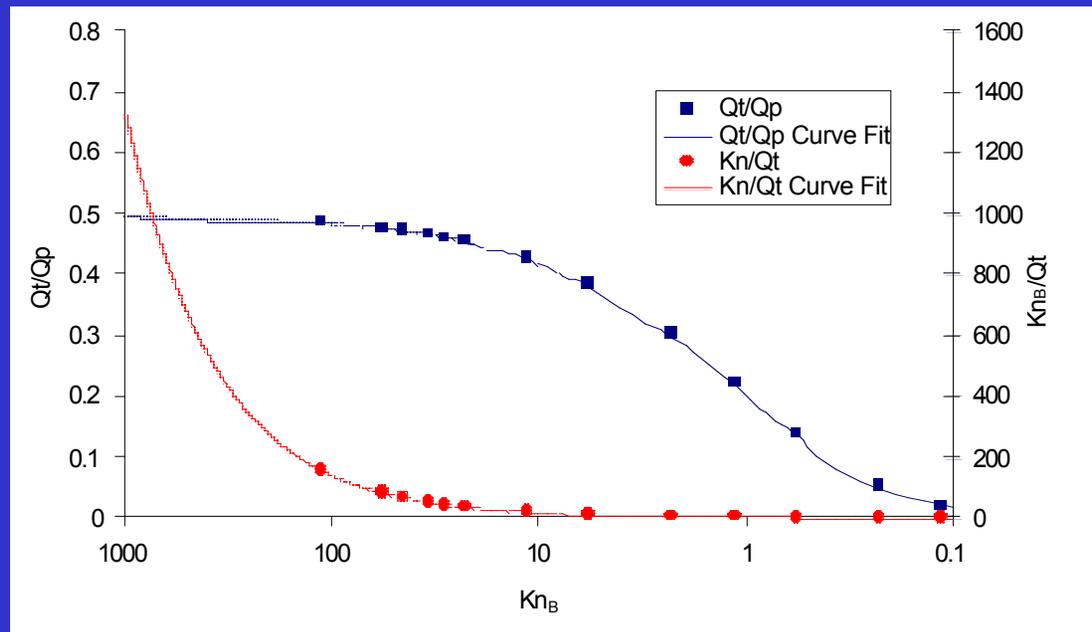
# Transitional Flow Formulation



Transitional Flow Equations:

$$\Delta p = p_{AVG} \frac{\Delta T}{T_{AVG}} \frac{Q_T}{Q_P} \cdot \kappa$$

$$M_i = \left[ \frac{p_{AVG} F A}{(2(k/m) T_{AVG})^{1/2}} \left( \frac{\Delta T}{T_{AVG}} \right) Q_T (1 - \kappa) \left( \frac{L_r}{L_x} \right) \right]$$

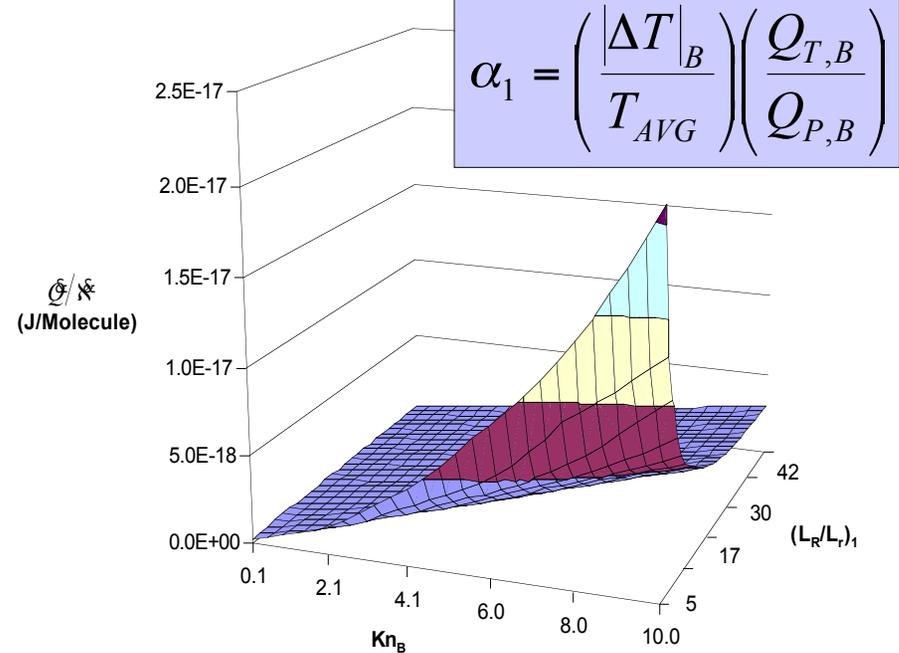
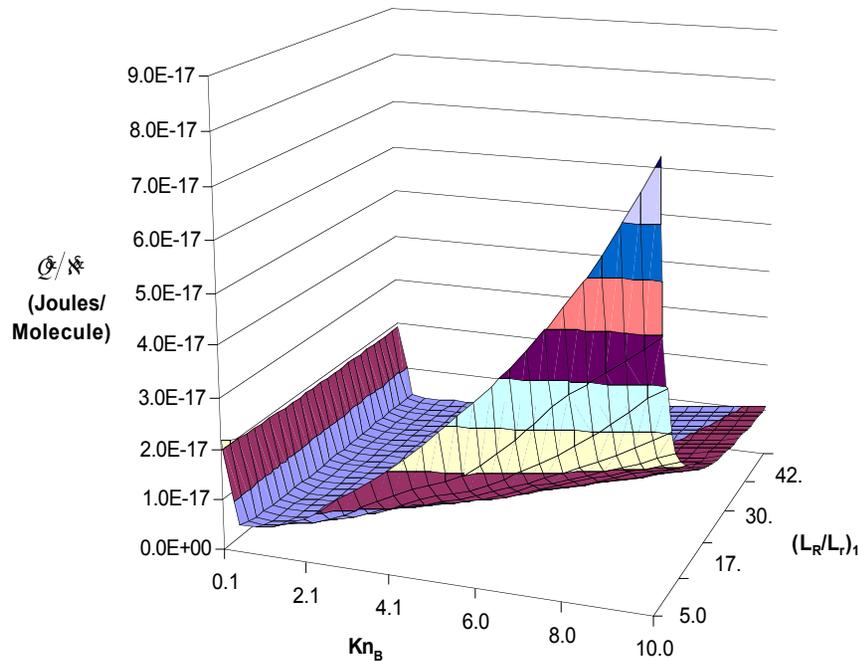


# Power Consumption Optimization Results

$\Delta T = \text{constant}$

$\Delta P = 10, L_r = 500\mu\text{m}$

$\alpha_1 = \text{constant}$



Kn low: capillary section is not very efficient

Kn high: constant number of stages  $\rightarrow$  energy consumption per unit number flux increases

$L_R/L_T$  low: little difference between the capillary and connector sections

$L_R/L_T$  high: constant number of stages  $\rightarrow$  energy consumption per unit number flux constant

Kn low: inefficiency counteracted by increasing  $\Delta T \rightarrow$  no large increase in the number of stages

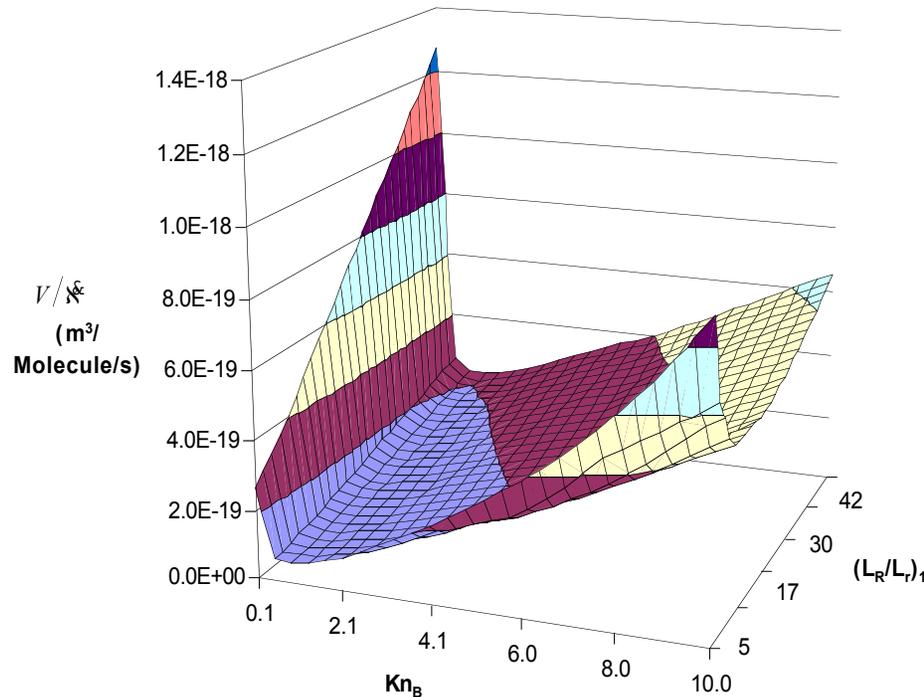
Kn high: same as  $\Delta T = \text{constant}$

$L_R/L_T$  low: same as  $\Delta T = \text{constant}$

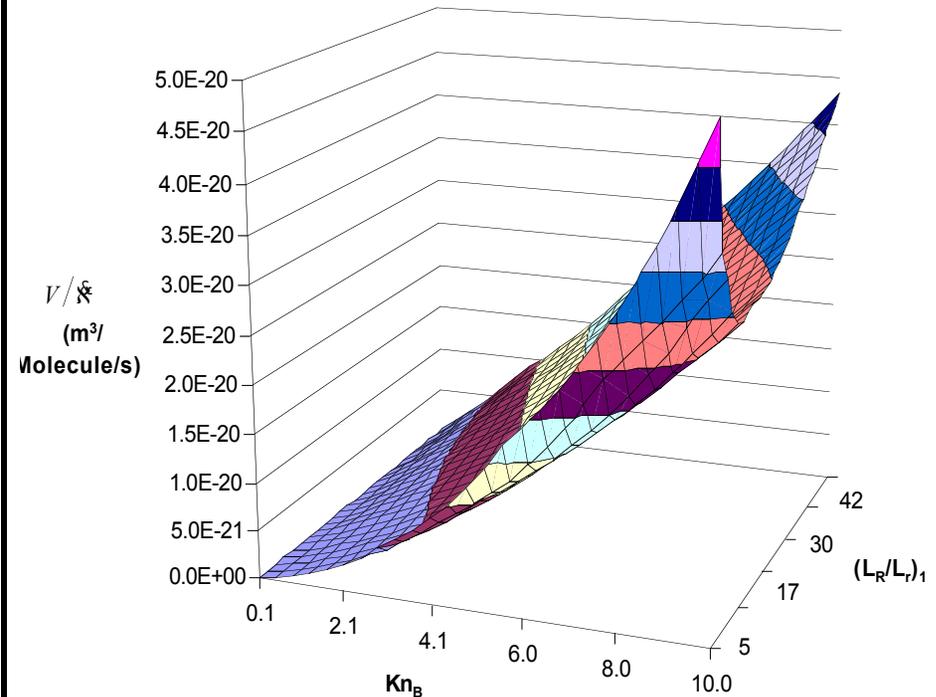
$L_R/L_T$  high: same as  $\Delta T = \text{constant}$

# Volume Optimization Results

$\Delta T = \text{constant}$



$\alpha_1 = \text{constant}$



$Kn$  low: capillary section is not very efficient

$Kn$  high: constant number of stages  $\rightarrow$  volume per unit number flux increases linearly

$L_R/L_T$  low: little difference between the capillary and connector sections

$L_R/L_T$  high: length of the connector is increasing linearly with  $(L_R/L_T)_1 \rightarrow$  increase linearly

$Kn$  low: inefficiency counteracted by increasing the temperature difference  $\rightarrow$  no large increase in the number of stages

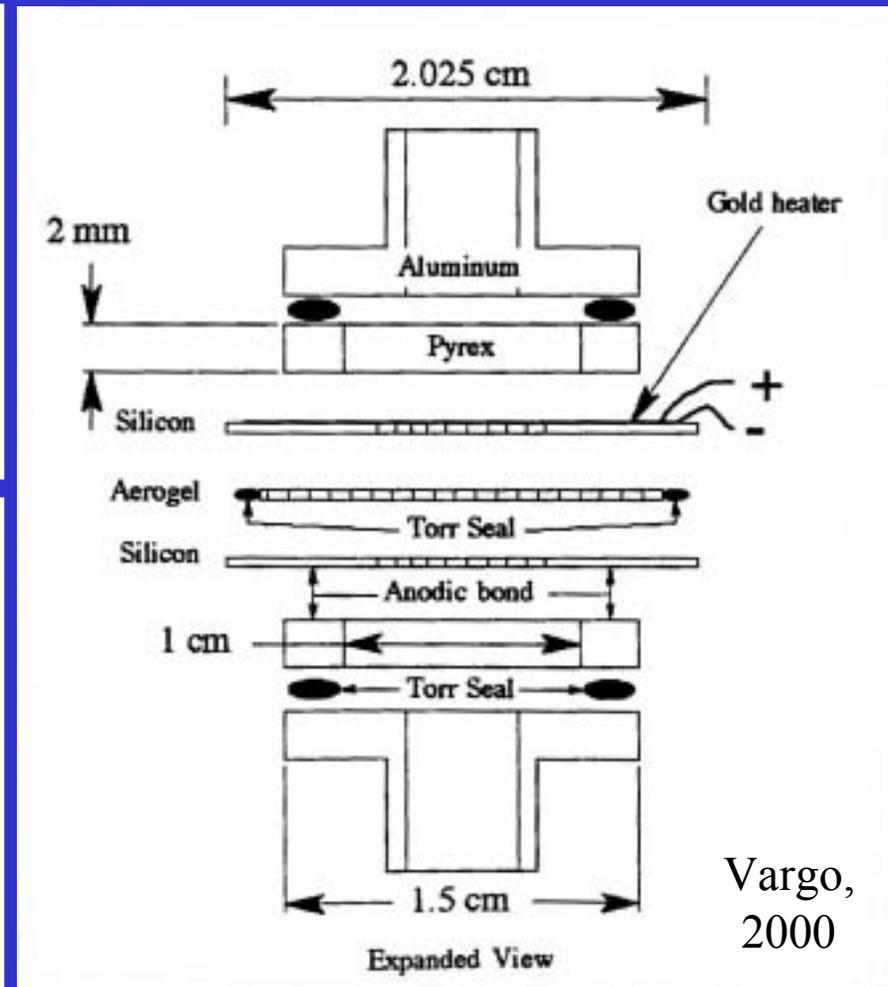
$Kn$  high: same as  $\Delta T = \text{constant}$

$L_R/L_T$  low: same as  $\Delta T = \text{constant}$

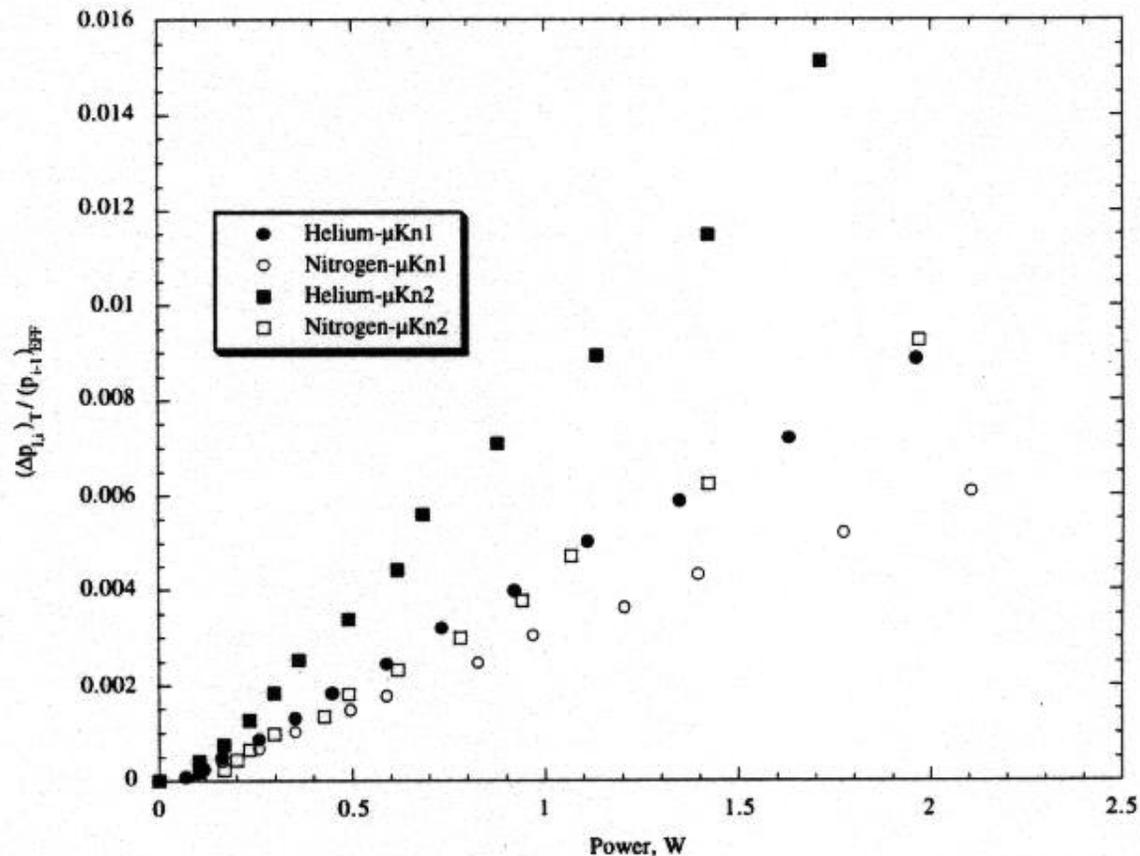
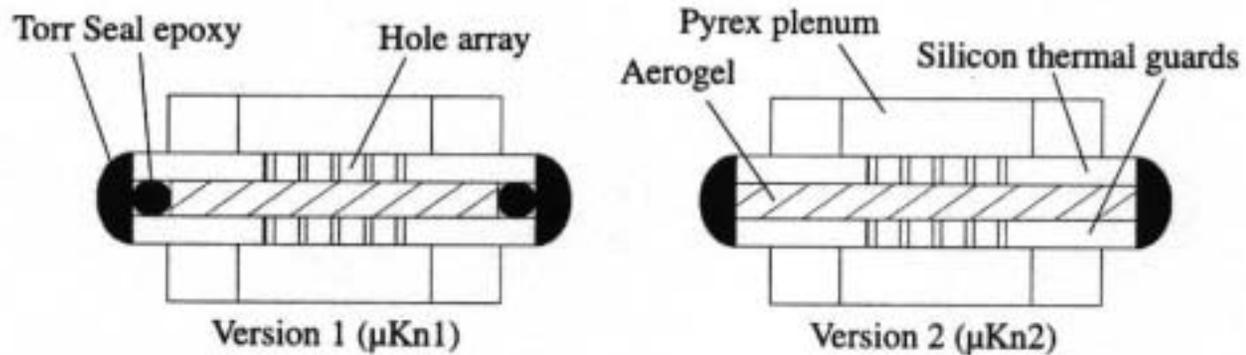
$L_R/L_T$  high: length of the connector is increasing linearly with  $(L_R/L_T)_1 \rightarrow$  increase linearly

# Previous Experimental Design

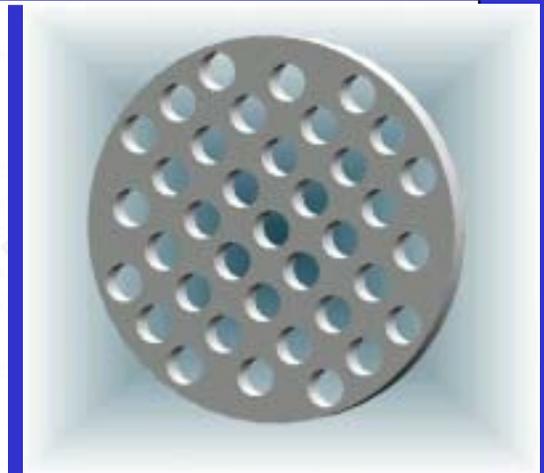
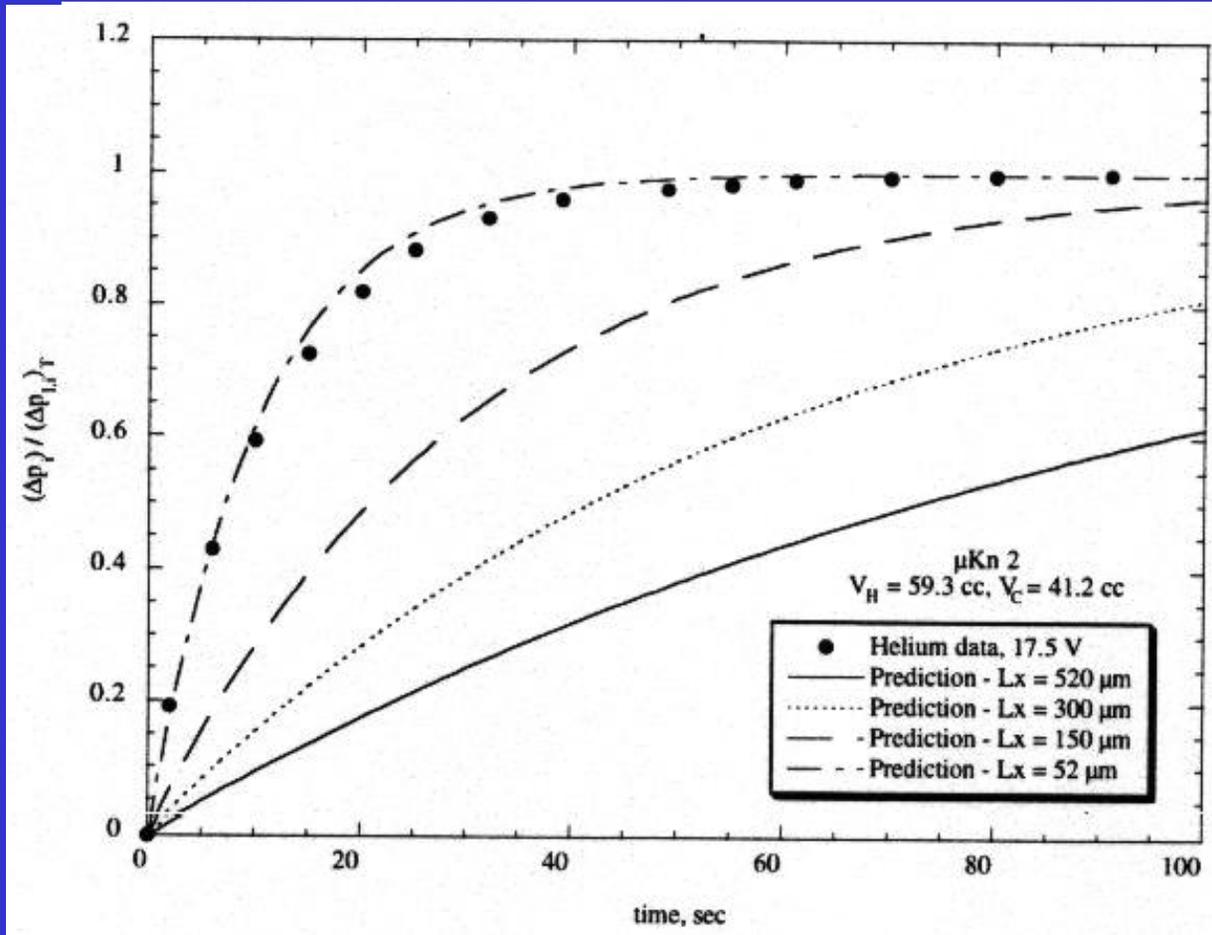
- Silicon Aerogel as Transpiration Membrane (0.6mm thick)
  - Silicon wafer with DRIE holes and thin film gold heater used to apply temperature gradient
  - Pyrex connector sections
- Proof of concept for multiple stages
  - Thermally efficient sealing identified as a major problem
  - Transitional flow analysis validated
  - Operation shown from atmospheric pressure down to several hundred Torr for several different working gases.



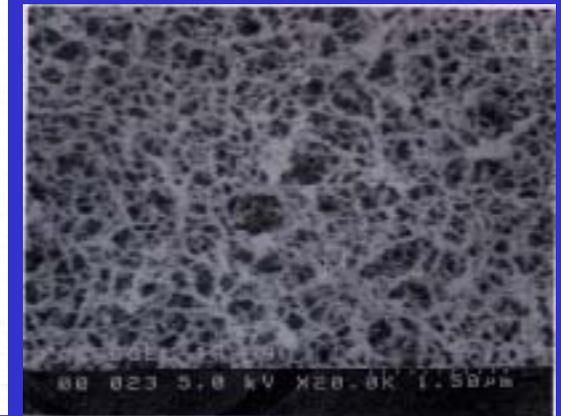
# Previous Results: Efficiently Sealing Membrane



# Previous Results: Validation of transitional flow model

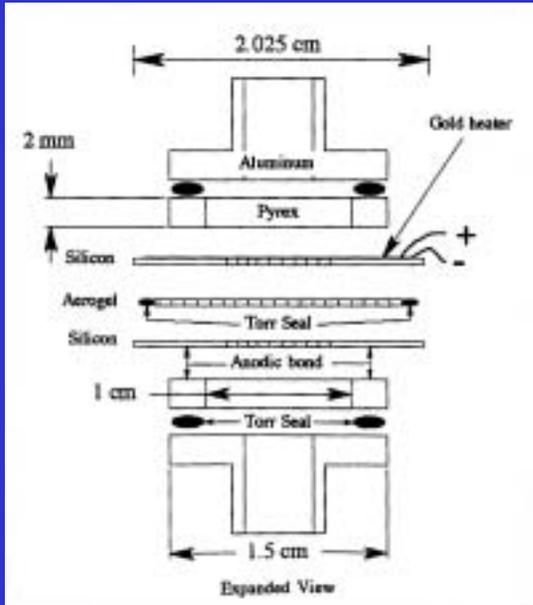


VS.



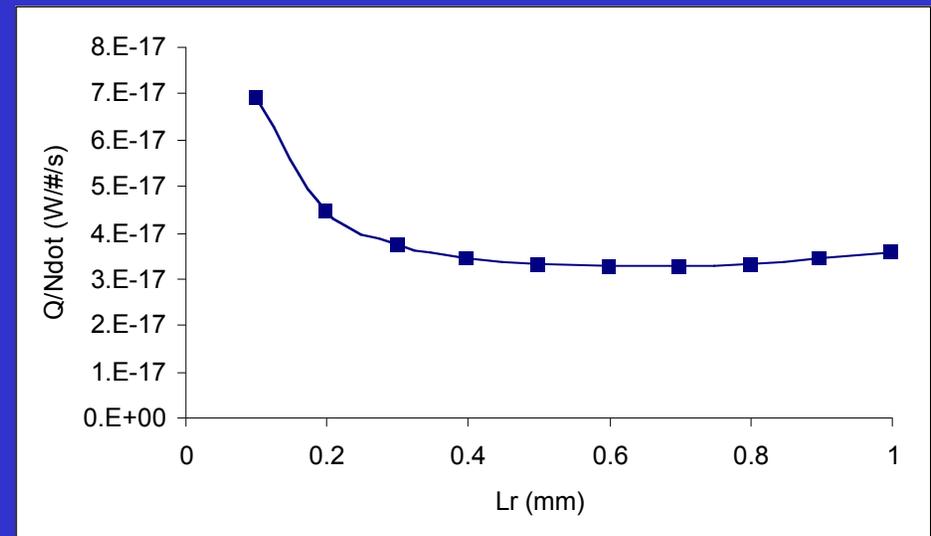
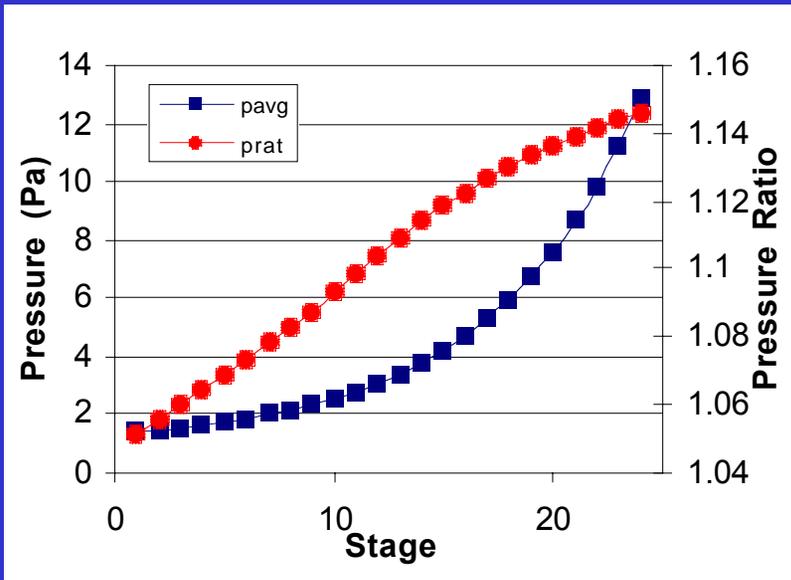
- Model adequate for performance estimation using aerogel
- 10x better flowrate than predicted using nominal pore size and membrane thickness

# Low Pressure Cascade Sizing Using $L_r = 10\text{nm}$



$\Delta T = 100\text{K}$   
 $L_r = 10\text{nm}$   
 (2% carbon doped aerogel)  
 $L_x = .55\text{ mm}$   
 $L_R = 5\text{mm}$   
 $L_X = 20\text{mm}$

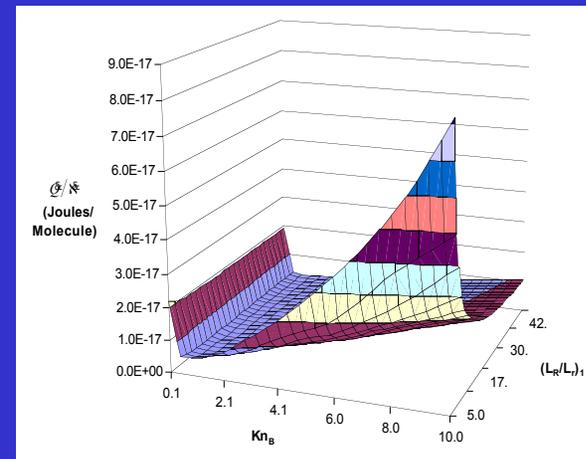
Number of Stages	24
Pressure Ratio	10 (10-100 mTorr)
<b>Flow Rate</b>	<b>6E13 (#/s) or 0.186 ml/s</b>
Volume	33 cm <sup>3</sup>
Power Consumption	1.5 W
<b>Energy Efficiency</b>	<b>2.5E-14 W/(#/s)</b>
<b>Volumetric Efficiency</b>	<b>5.5E-19 m<sup>3</sup>/(#/s)</b>



# Considerations to Optimize Design for Low Pressure Applications

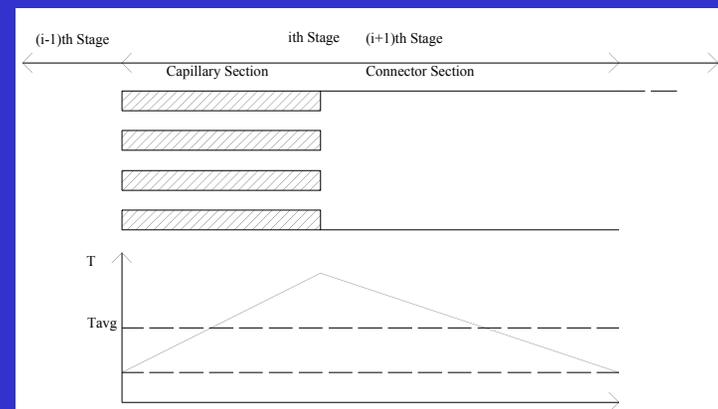
## Optimize Capillary Pore Diameter

- $Kn \sim 1$  is optimum in capillary pores, using aerogel pores  $\rightarrow Kn = 4.6E5$
- By boring holes in the aerogel transpiration membrane the pore diameter can be optimally sized



## Impose required temperature gradient

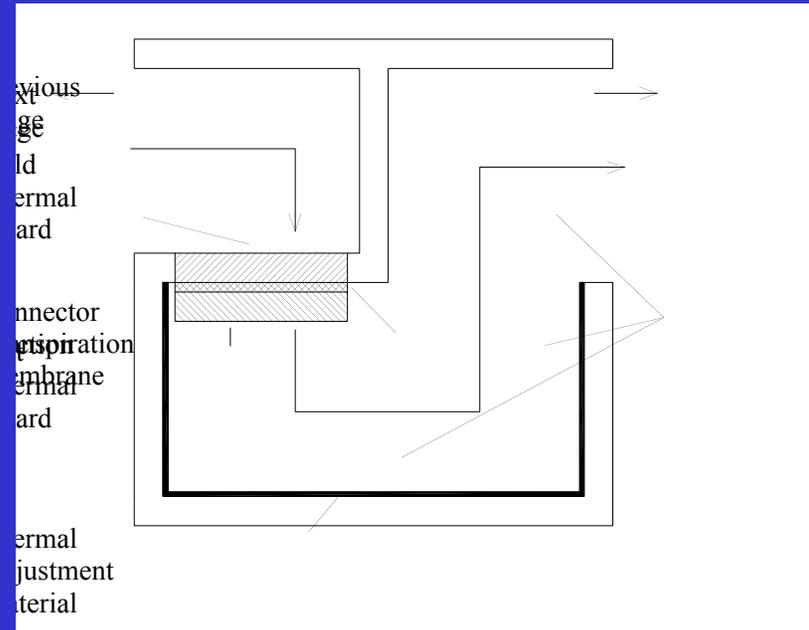
- At low connector  $Kn$  the gas is not uniformly hot at the hot side of the pores due to direct reflections from connector walls
- Add thermal adjustment material



# Performance Using Optimized Pore Diameters

## Modifications:

- 1.) Bore Optimized Holes in Aerogel Substrate
- 2.) Add Thermal Adjustment Material



Cascade	$L_r$ (m)	$L_x$ (m)	$L_R$ (m)	$L_X$ (m)
10-100 mTorr	2.5E-04	5.0E-04	5.0E-03	2.0E-02
100 mTorr - 1Torr	2.5E-05	5.0E-04	2.8E-03	2.0E-02
1Torr-10Torr	2.5E-06	5.0E-04	2.7E-03	2.0E-02
10Torr-760 Torr	1.0E-08	5.0E-04	1.3E-03	5.0E-03

# Low Pressure Performance Comparison

## •Performance Increases Due to New Design

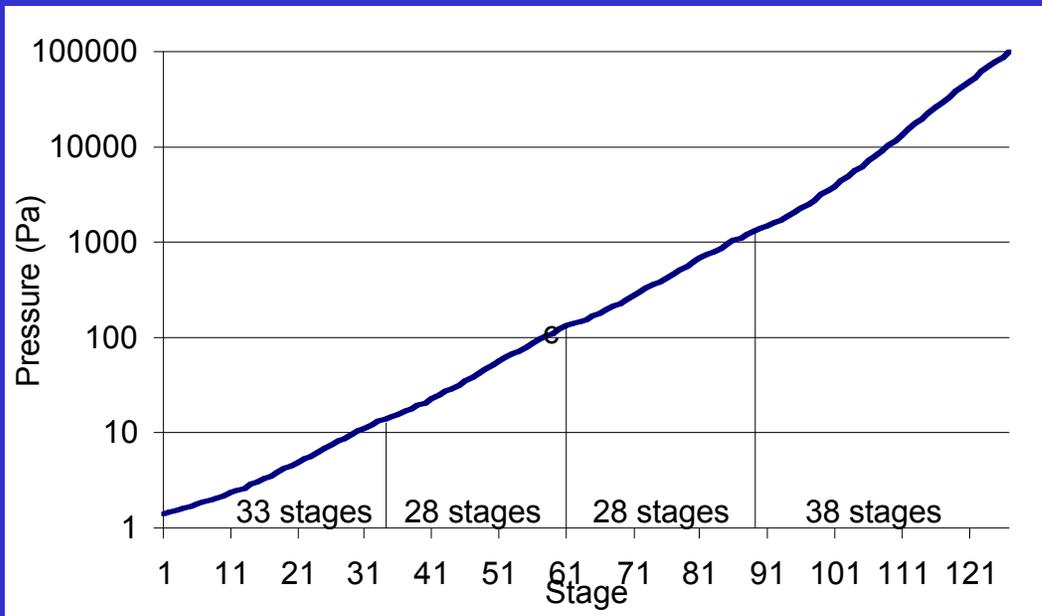
Number of Stages	24
Pressure Ratio	10 (10-100 mTorr)
Flow Rate	6E13 (#/s)
Volume	33 cm <sup>3</sup>
Power Consumption	1.5 W
Energy Efficiency	2.5E-14 W/(#/s)
Volumetric Efficiency	5.5E-19 m <sup>3</sup> /(#/s)

Number of Stages	33
Pressure Ratio	10 (10-100 mTorr)
Flow Rate	3E16 (#/s)
Volume	45 cm <sup>3</sup>
Power Consumption	1.1 W
Energy Efficiency	7.E-17 W/(#/s)
Volumetric Efficiency	1.5E-21 m <sup>3</sup> /(#/s)

- increased pore diameter → increased conductance
- increased conductance → increased mass flow
- decreased  $\lambda$ , Kn → decreased TMPD
- decreased pressure ratio → increased number of stages
- Net Results: more stages and volume, less power and volume/ upflow

# Performance of New Design

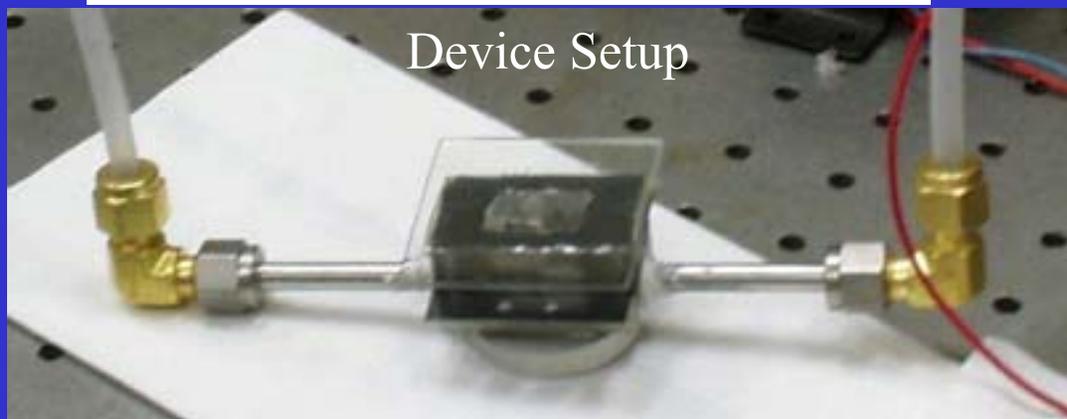
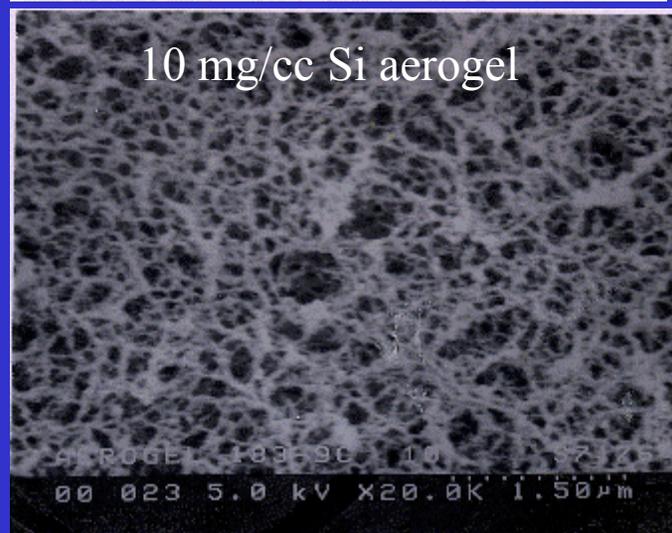
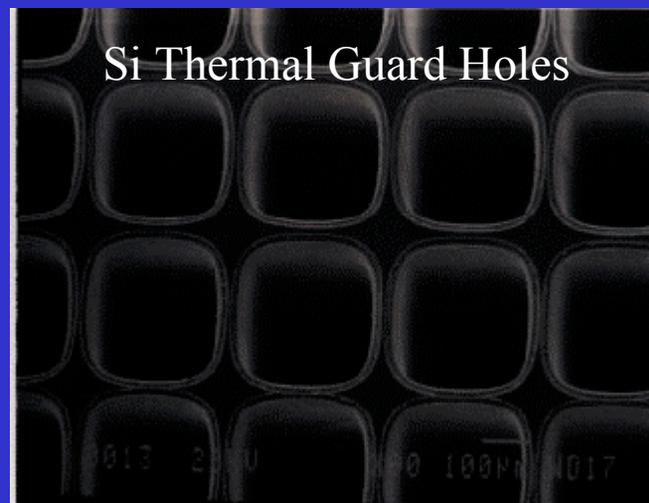
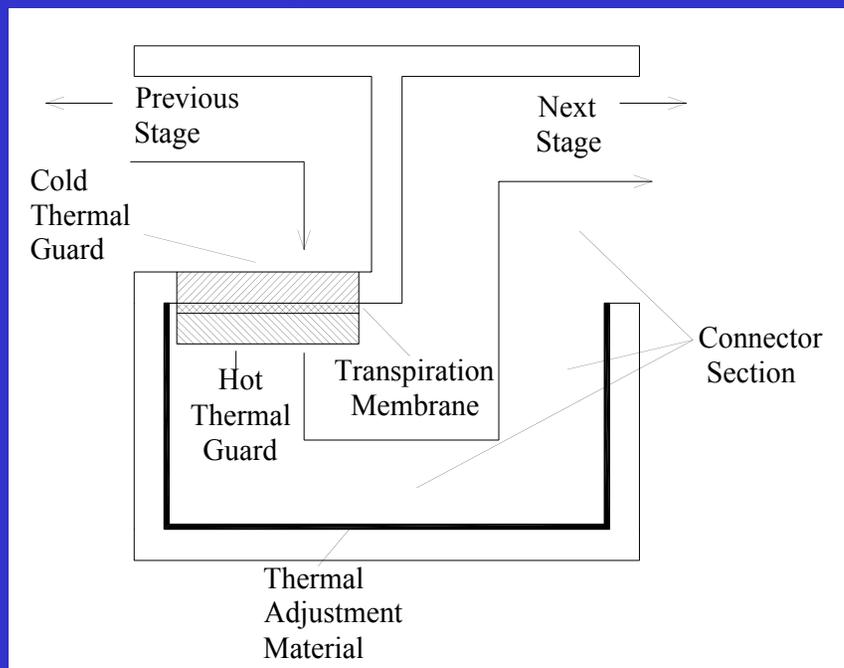
Cascade	Volume (cm <sup>3</sup> )	Power (W)
10-100 mTorr	45.1	1.07
100mTorr-1Torr	13.0	0.297
1Torr-10Torr	11.8	0.268
10Torr-760Torr	5.26	0.92
Total	75.2	2.56



Power Efficiency	8.5E-17 W/(#/s)
Volumetric Efficiency	2.5E-21 m <sup>3</sup> /(#/s)

# Status of Experimental Work

- One stage device constructed and testing is ready to begin



# Conclusions

- Optimum operation (based on thermal and volumetric efficiency) occurs at Capillary Kn  $\sim 1$ .
- Pore sizes must be optimized for low pressure application.
- Thermal adjustment material must be added at low pressures
- 10 mTorr identified as the lowest practical pressure attainable with a MEMS Knudsen Compressor.

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